A SELECTIVE EDITING METHOD CONSIDERING BOTH SUSPICION AND POTENTIAL IMPACT, DEVELOPED AND APPLIED TO THE SWEDISH FOREIGN TRADE STATISTICS

Invited Paper

Submitted by Statistics Sweden

Summary: A score function computed as a weighted geometric mean of measures of suspicion and potential impact has successfully been implemented in the editing process of the Swedish foreign trade statistics. There are well over 10,000 statistical table sums to be produced and published each month. We have developed a formula with which the tolerable impact of the errors on the statistics on all aggregation levels and sizes of table sums can be expressed in one single variable. The survey managers have set the values of six constants that reflect the importance of potential errors on different aggregation levels and sizes of the sums.

The method needs relevant and accurate medians and quartiles for homogenous groups. For example, we have to decide whether we shall use current or historical data, the minimum number of observations to be used, and whether to use weighted or unweighted quartiles. In total we have ten different specifications to decide on to get the best possible performance. Hundreds of thousand different combinations of specifications were tested on raw and edited historical data.

The sum of changes in invoiced value was 494 MSEK for the old method and 819 MSEK for the new method, when they were used in parallel in December 2003. The hit rate has increased from about 40 percent to 65 percent. Guided by this initial analysis the method was implemented in production in January 2004. Process data are now produced every month in a continuous search for best specifications.

I. INTRODUCTION

1. Intrastat is a survey created for Member States of the European Union (EU) that covers trade of goods among States within the EU. Each month some 350,000 data are collected from enterprises in a total census with cut-off, by Statistics Sweden. One editing process is the checking of unit prices. In this editing process one criterion for selecting data to be verified is the potential impact on the summed values of trade in the published tables and the other criterion is our suspicion that a data value is erroneous.

2. The foreign trade statistics are published for in- and outflow at the 6-digit classification according to the CN-nomenclature\(^2\) and higher aggregation levels. Statistics are also published with the

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2\ The Combined Nomenclature has 8 digits. The first 2, 4 and 6 digits form relevant groups of goods.
alternative item classification SITC\(^3\) and for each of the countries in the EU. There are well over 10 000 table sums per month in the official database. In the paper we describe a formula for reducing the problem of deciding the tolerable impact on all these published statistics into a choice of six constants.

3. The method needs relevant and accurate medians and quartiles for homogenous groups. Some issues are: Should we use historical data or only current data, what is the minimum number of observations needed, should we calculate weighted or unweighted quartiles, is it necessary to split data into inflow and outflow of goods? Detailed grouping is in conflict with demand on a minimum amount of data for computing quartiles and medians, a problem that also involves the number of months of historical data. In cases when there are enough data for detailed grouping, one issue is if one shall use information on all such levels or only on the most detailed level.

4. Statistics Sweden has saved raw and edited data since the year 2000. In the data there is information on 8-digit CN (i.e. more detailed than what is published), country, enterprise, year and month. We have tested the editing method with ten specification parameters on the data to find out which set of values is the best. Guided by this initial analysis the method was implemented in production in January 2004. We continuously run tests by changing some of the specifications almost every month. Process data are produced in a search for best specifications.

II. SUSPICION

5. The median and quartiles are fundamentals in modern editing procedures, see Hidiroglou and Berthelot (1986). We define suspicion as the distance between an observation and the closest of the upper and lower quartiles divided by the inter-quartiles distance. Since ratios like unit prices by nature have skewed distributions we take the logarithm of the unit prices.

Let \( UP_i \) be the unit price for an observation \( i \) in our current data, i.e. \( UP_i = \frac{\text{Invoiced value}_i}{\text{Quantity}_i} \).

Let \( UP_{Q1}(i) \) and \( UP_{Q3}(i) \) be the lower and the upper quartiles for unit prices computed on historical data – or computed on all the data for the current month – that belong to a “homogenous group”, to which the observation \( i \) also belongs. The “homogenous group” is explained in sections 20-27.

We define Suspicion as:

\[
\text{Suspicion}_i = \begin{cases} 
\frac{\log(UP_{Q3}(i)) - \log(UP_i)}{\log(UP_{Q1}(i)) - \log(UP_{Q3}(i))} & \text{if } UP_i < UP_{Q1}(i) \\
\frac{\log(UP_i) - \log(UP_{Q1}(i))}{\log(UP_{Q1}(i)) - \log(UP_{Q3}(i))} & \text{if } UP_i > UP_{Q3}(i)
\end{cases}
\] (1)

Suspicion is zero otherwise. When the quartile distance is zero, the denominator is replaced by a fixed value or a value proportional to \( UP_{Q2}(i) \), the median unit price of similar goods.

III. POTENTIAL IMPACT IN A MULTI-PURPOSE SURVEY

6. In order to detect errors in data that have significant potential impacts on the results we start out from the difference in Invoiced value (SEK) between observed value and an expected value, given the quantity. We use the median of unit prices, \( UP_{Q2}(i) \), multiplied by Quantity, as the best expected value. Notice that an error in the variable Quantity results in a potential impact measured in value.

\(^3\) Standard International Trade Classification
7. An erroneous observation has potential impact on several domains of study in the published database. Therefore we first have to construct a Potential impact variable for each domain. The Potential impact is the ratio of estimated error to the "expected" sum for the domain of study.

\[
\text{Potential Impact}_i^g = \frac{|\text{Invoiced value}_i - \text{Quantity}_i \cdot \text{UP}_{Q2}(i)|}{\sum_{k \in g} \text{Invoiced value}_k^*} \quad \text{if } i \in g
\]

where \( g \) denotes a domain of study.

The median value \( \text{UP}_{Q2}(i) \) is computed on a homogenous set of data, independent of \( g \), that makes the median a good predictor of the unit price for the object \( i \).

The sum \( \sum_{k \in g} \text{Invoiced value}_k^* \) is a sum over 24 months of Invoiced values for the domain of study \( g \).

When \( g \) is a domain with varying total from month to month, without a stable seasonal pattern, we think it is better to use an annual total. If, on the other hand, the domain of study \( g \) has a distinct seasonal pattern it might be better to compute this sum only on the current month and/or the same month the last years. To simplify the method we have made the choice to use annual data.

8. There are two reasonable demands on a comparison of acceptable impacts on two domains of study \( g_1 \) and \( g_2 \):
   
   - **Size:** If \( g_1 \) and \( g_2 \) are two domains of study formed by the same classification variables, for example by in-/out-flow and 2 digit SITC, we tolerate a relatively smaller impact of errors on \( g_1 \) if \( g_1 \) over the last two years has had a larger sum of trade than \( g_2 \).
   
   - **Importance of classification variable:** If \( g_1 \) and \( g_2 \) are two domains of study formed by different classification variables, but \( g_1 \) and \( g_2 \) over the last two years have had the same size of the sum of trade, we tolerate a relatively smaller impact of errors when the classification variables are more aggregated. 2-digit SITC is more aggregated than 3-digit SITC and 6-digit CN.

9. After consultation with survey managers we have settled the importance of size by the constant \( f \) and the relative importance for the five classification variables total arrivals/dispatches, 2-digit and 3-digit SITC, 6-digit CN and a set of important 8-digit CN-codes. The importance of these five are defined by a relative factor \( O_v, v=1\ldots5 \). Total arrivals/dispatches is given the factor \( O_1=0.1 \) and the other five higher values are set subjectively by the management according to their view of the relative importance of different levels of aggregations.

10. We have constructed this measure of potential impact.

\[
\text{Potential Impact}_1 = \max_{\text{over} v=1\ldots5} \left\{ \frac{|\text{Invoiced value}_i - \text{Quantity}_i \cdot \text{UP}_{Q2}(i)|}{\sum_{k \in g_v} \text{Invoiced value}_k^*} \cdot \frac{1}{O_v} \cdot 10^{\log \left( \sum_{k \in g_v} \text{Invoiced value}_k^* \right)} \right\}
\]

\[
= \left| \text{Invoiced value}_i - \text{Quantity}_i \cdot \text{UP}_{Q2}(i) \right| \cdot \max_{\text{over} v=1\ldots5} \{ R_v(i) \}
\]

\[
\text{where } R_v(i) = \frac{1}{\sum_{k \in g_v} \text{Invoiced Value}_k^*} \cdot \frac{1}{O_v} \cdot f \cdot 10^{\log \left( \sum_{k \in g_v} \text{Invoiced Value}_k^* \right)}
\]

Here we have taken the maximum over the five classifications, \( v=1\ldots5 \). The sum of impacts for the five classifications might be a more relevant function.
Our choice of values for size effect \( (f) \) and for relative importance of aggregation variables \((O_v)\) has made 6-digit CN, 3-digit SITC and 2-digit SITC approximately equally important when we judge the impact of a potential error. This can be seen in Table 1.

**Table 1.** The level of aggregation \((v)\) on which the reported lines had the greatest potential impact. Data from reference month October 2004. The size-parameter \( f=4 \).

<table>
<thead>
<tr>
<th>Level of aggregation ((v))</th>
<th>Importance of classification variable (O_v)</th>
<th>Number of observations flagged</th>
<th>Number of observations not flagged</th>
<th>Number of lines not possible to check</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Other CN8</td>
<td>---</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Important CN8</td>
<td>1.5</td>
<td>13</td>
<td>4,871</td>
<td>0</td>
<td>4,884</td>
</tr>
<tr>
<td>CN6</td>
<td>1.0</td>
<td>600</td>
<td>145,761</td>
<td>59</td>
<td>146,420</td>
</tr>
<tr>
<td>SITC3</td>
<td>0.3</td>
<td>488</td>
<td>137,340</td>
<td>17</td>
<td>137,845</td>
</tr>
<tr>
<td>SITC2</td>
<td>0.2</td>
<td>390</td>
<td>90,605</td>
<td>12</td>
<td>91,007</td>
</tr>
<tr>
<td>Arrivals/Dispatches</td>
<td>0.1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

**IV. SUSPICION FOR ERRORS IN INVOICED VALUE AND QUANTITY**

11. We soon learned that a symmetric search for errors in the variables *Invoiced value* and *Quantity* results in many more errors found for *Quantity* than for *Invoiced value* (see Table 2 in section 15). As the primary objective of the statistics is to compute the summed value of foreign trade, we would like to prioritize the search for errors in *Invoiced value*. The unit prices bear no information on which of the two variables is in error. We therefore have constructed a rough indicator telling which of the two variables is most likely to be erroneous.

12. First we compute a measure of suspicion for the *Invoiced value* as such to be erroneous, i.e. without taking the *Quantity* into account. We do this by comparing the observed value to the quartiles, based on historical data, in the same way as in (1). Here it is important to include the variable Enterprise in the definition of the homogenous groups[^4]. The same method is applied to the variable *Quantity*.

13. We then divide the suspicion for *Invoiced value* with the suspicion for *Quantity*. If suspicion for *Quantity* is zero, which it is for about half of the observations, it is replaced by a small number. Visually we have found that the following expression is linearly correlated to the proportion of errors in *Invoiced value*. This is our measure of suspicion for *Invoiced value* over *Quantity*.

\[
\text{Suspicion}_i = \begin{cases} 
1 & \text{if } \text{Suspicion}(\text{Invoiced value}_i) \leq \text{Suspicion}(\text{Quantity}_i) \\
1 + \log \left( \frac{\text{Suspicion}(\text{Invoiced value}_i)}{\text{Suspicion}(\text{Quantity}_i)} \right) & \text{otherwise}
\end{cases}
\tag{5}
\]

[^4]: Enterprises can chose between different ways to deliver information to Statistics Sweden. For one method each row on an invoice makes one observation, for another method data for one month are aggregated to a sum for in-/out-flow, country and 8 digit CN-code.
V. SCORE

We compute the score as a weighted geometric mean of the three variables we now have defined in (1), (2) and (5):

\[ Score_i = Suspicion_i \cdot \left( \text{Potential Impact}^{P_{Susc}} \right)^{P_{Imp}} \cdot \left( \text{Suspicion}_\text{Va}_i \right)^{P_{Susc, Va}} \]  

(6)

In figure 1 it is illustrated that the boundary of the acceptance region is a line in the log-scale for Suspicion and Potential Impact, when \( P_{Susc, Va} = 0 \). The slope is \(-1/P_{Imp}\). The ordinate in origin depends on the number of observations we can afford to verify.

VI. STUDY

14. Statistics Sweden has saved raw and corrected data for all months since the year 2000. We have used subsets of these data for searching for the best specification parameter values for our editing system. First we used data for seven months 2003 to make a rough limitation of the value ranges. Then we used 12 month of data for 2002 to search for the best values within a more limited set.

15. More often there are errors in the variable Quantity than in Invoiced value. Furthermore the errors are of larger magnitude for Quantity. In the study we omitted the observations where one or both of the variables were reduced with a factor 1/10,000 or increased with a factor 10,000.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Proportion of data with errors (%)</th>
<th>Proportion of total impact of errors (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quantity</td>
<td>32.9</td>
<td>99.5</td>
</tr>
<tr>
<td>Invoiced value</td>
<td>7.7</td>
<td>0.5</td>
</tr>
<tr>
<td>One or the other or both</td>
<td>38.2</td>
<td>100.0</td>
</tr>
</tbody>
</table>

16. A question left open for discussion is whether we will be misled when we try to construct a new editing method by analysis of data that has been flagged by the old method. Is our conclusion concerning the optimum parameter values dependent on the method that has been used to flag the observations? Despite these concerns the method was implemented in January 2004, guided by the initial results of this study. Extensive process data are now produced every month in a continuous search for best parameter values.

17. We have used the following indicators to evaluate the performance of the editing method for different parameter values:

1. \( \text{Imp(Invoiced value)} = \text{Maximum impact on published statistics due to errors in the variable Invoiced value} \)

2. \( \text{Imp(Invoiced value, Quantity)} = \text{Maximum impact on published statistics due to errors in the variable Invoiced value and/or the errors in the variable Quantity} \)
3. \( \text{Imp}(\text{Invoiced value, Quantity}/100) = \) Maximum impact on published statistics due to errors in the variable \text{Invoiced value} and/or one hundredth of the errors in the variable \text{Quantity}.

4. \( \text{Diff}(\text{Invoiced value, Quantity}) = \) Corrections on the variables \text{Invoiced value} and \text{Quantity}, transformed to Value

5. \( \text{Hit rate}(\text{Invoiced value}) = \) Hit rate for any error in \text{Invoiced value}.

6. \( \text{Hit rate}(\text{Invoiced value, Quantity}) = \) Hit rate for any error in \text{Invoiced value} and \text{Quantity}

**STEP 1. DATA FOR COMPUTATION OF QUARTILES**

### Current data or historical data

18. A primary question in designing an editing method is whether current data or historical data should be used for computing the quartiles, including the median, that are used in the measures of suspicion and potential impact. For several product groups there are seasonal variations in both quantities and unit prices. Freshness of the data is therefore a good characteristic. Advantages of historical data are primarily that we can use as many objects as we may wish and secondary that the data are verified.

19. We have tested current unedited monthly data as well as one, two and three years of old data, i.e. 12–36 times as many observations. Here it is very significant that 1-3 years of monthly data are required to construct an efficient editing method. The study suggests using two years of monthly data.

### Grouping and number of historical observations

20. On which group do we compute quartiles in order to get both relevant and accurate measures of mean and dispersion for each observation \(i\)? Relevance depends on the homogeneity of the group, whereas accuracy depends both on homogeneity and number of observations. Historical data give, by nature, less relevant but more accurate estimates than current data.

21. We start off with the 6-digit CN-groups as the most heterogeneous groups we can ever accept. Then there are several possible variables to use for splitting these into more homogenous groups – with less objects in each. We have:

- 8-digit CN-code
- In/Out flow
- Enterprise
- Country (from which Sweden imports or to which Sweden exports)
- Last twelve months (in case several years of historical data are used)

22. If we split data into a cross-classification using all these variables, there will be none or only a few observations in many cells. Therefore we fix a minimum number of observations for the computation of quartiles, \(N_{\text{Obs}}\). For a given order of the splitting variables we split each CN6-group hierarchically as long as there are more than \(N_{\text{Obs}}\) observations in the data. The priority order of the five splitting variables is also to be decided.

23. Choosing the one variable that gives the most homogenous groups is much the same problem as finding the variable that has the highest partial F-value in an analysis of variance with unit price as dependent variable and CN6 already in the model. Here we set a restriction that when there are fewer than \(N_{\text{Obs}}\) observations in a group the within sum of squares is computed around the average on the CN6-level.

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5 Errors in \text{Quantity} are much more frequent and larger in size than errors in \text{Invoiced Value}. Division of the \text{Quantity} errors makes them comparable in this aspect.
Table 3. Degree of explanation (%) of total variation for the variable logarithm of unit price

<table>
<thead>
<tr>
<th>Minimum number of observations (N_Obs)</th>
<th>5</th>
<th>10</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td>Enterprise</td>
<td>49.3</td>
<td>41.9</td>
<td>17.9</td>
</tr>
<tr>
<td>Country</td>
<td>9.0</td>
<td>8.3</td>
<td>5.4</td>
</tr>
<tr>
<td>8-digit CN-code</td>
<td>5.6</td>
<td>5.5</td>
<td>4.8</td>
</tr>
<tr>
<td>In/Out-flow</td>
<td>4.0</td>
<td>4.0</td>
<td>3.6</td>
</tr>
</tbody>
</table>

24. The table indicates that editing should be made individually for each enterprise, if we have a lot of historical data. When we demand 50 instead of five observations for the computation, the power of this variable has declined most because there are so many different values. Beside this variable there seem to be little gain in splitting a 6-digit CN group.

25. There are interactions between the three parameters N_Obs, Priority_order and number of years of monthly data. If we have a large number of historical data, say three years, we can use a higher limit for the number of observations needed in the computations, N_Obs. The splitting variable Enterprise takes 16,000 values while the variable arrivals/dispatches only takes two, and therefore the second works equally well with a small and a high N_Obs.

26. For all the six indicators the best value of N_Obs is very clearly 2, which is an extreme value. We tried values from 2 to 64. Our conclusion is that it is important to split the population into as homogenous groups as possible. We have considered the risk that a systematic erroneous behaviour by enterprises can slip into the data if only two historical observations are needed per enterprise for computation of quartiles. We therefore suggest a value for N_obs in the range 4–8.

27. A priority order starting with Enterprise and Country might lead to a high hit rates and high total impacts in the search for errors, but for several combinations of other parameter values it has also lead to bad performance of the method. Setting the variables in the following order gives robust and good results: 8-digit CN-code, In/Out-flow, Enterprise, Year and Country. We have also tested, with this order, if the last variable Country contribute to the potential impact of the flagged observations, and it did.

Weighted or un-weighted quartiles

28. The historical data that will be used for computing quartiles for unit prices are very skewed on the variable Quantity. We will certainly get different results if we weight by Quantity or not. In some cases, especially if we use current un-edited data where there are errors, one or a few observations can influence the results substantially. For this reason we try a truncated Quantity as a weighting variable. The question of weighting interact with the choice of N_Obs. With very few observations in a group it might be better to compute quartiles with no weighting.

29. For the Hit rate indicators and the pure difference indicator Diff(Invoiced value, Quantity) the best choice is not to weight. For hit rates this is understandable since all errors contribute equally much. When we want to detect errors that have a large impact on the summed values the best choice is to weight by Quantity, and preferable truncated for the largest values.

STEP 2. DEFINITION OF SUSPICION AND POTENTIAL IMPACT

Detail of grouping

30. When there are enough data to compute quartiles for several or all levels of groupings there is also a question if only the quartiles for the most detailed grouping should be used or if there is valuable

6 All orders have not been tested.
information on more aggregated levels. Beside defining Suspicion and Potential impact with the most
detailed splitting we have also computed them as averages over all possible splittings. The study did not
yield a clear recommendation. Potential impact can preferable be computed with the most detailed
splitting, while Suspicion rather should be computed as a mean of all possible splitting.

**Addition when the quartile distance is zero**

31. Hidiroglou and Berthelot propose that a fraction of the median replaces the quartile distance
when the quartile distance is smaller than this fraction of the median. They propose the fraction 0.05.
Since we analyze the logarithms of the unit prices, a one unit difference at any level on this scale means
the same relative difference in unit prices. This would imply that the quartile distance should be replaced
by a constant rather than by a fraction of the median. We tried several alternatives but found that 5-30%
of the median is the best.

**Suspicion versus probability of error**

32. We want to pick out the set of observations that have the largest deviations between raw and
corrected *Invoiced values*, valued by our formula (2).

Let us look at this problem from a probabilistic point of view. Assume we know
the probability of error and the size of the potential error. Then we want to
maximize the sum of products of probability of error and the potential impacts. Ideally we
therefore want our variable Suspicion to be correlated with probability of error.
The diagram shows that this is not the case.

![Figure 2. Hit rate versus Suspicion](image)

Footnote: Data have been sorted by Suspicion and aggregated into groups of
50 observations. Hit rate was computed as the proportion among the 50
observations in each group that had corrected data.

33. We have tested a few transformations of Suspicion. The simple transformation that Suspicion is
unchanged up to 4, but the excess over 4 is reduced to 20 %, has worked well. This is especially so for
the potential impact-indicators. For the Hit rate indicators a transformation should not be done, which is
understandable as this measure is based on hit only – not the size of error.

**STEP 3. RELATIVE WEIGHTS FOR SUSPICION AND POTENTIAL IMPACT**

34. The best choice of the relative weights $P^{\text{Imp}}$ and $P^{\text{Susp}_{\text{Va}}}$ highly depends on the choice of indicator.
If we want high hit rates, no or little weight should be laid on Potential impact, but if we want to detect
errors in *Invoiced value* with high impact $P^{\text{Susp}_{\text{Va}}}$ should be high.
Imp \((Invoiced\ value)\)

If we want to find observations with as large impact on the variable \(Invoiced\ value\) as possible we should select parameter values for \(P_{Imp}\) and \(P_{Susp.Va}\) as for example 1 and 4 or 2 and 8.

Imp \((Invoiced\ value,\ Quantity/100)\)

If we want to get large impacts of the editing of both the variable \(Invoiced\ value\) and the variable \(Quantity\), there seems to be a larger tolerance for different parameter values. \(P_{Imp}\) and \(P_{Susp.Va}\) should be for example 1 and 2-4 or 2 and 4-8.

Diff \((Invoiced\ value,\ Quantity)\)

If we want to find summed corrections we should not be concerned for the suspicion for errors in \(Invoiced\ value\).

Hit rate \((Invoiced\ value,\ Quantity)\)

The best parameter values to choose for getting highest overall hit rates are \(P_{Imp}\) around 0.3 and \(P_{Susp.Va}\) to zero.

Hit rate \((Invoiced\ value)\)

If we want high hit rates for the variable \(Invoiced\ value\) we should consequently disregard the potential impact and set the parameter \(P_{Susp.Va}\) to 3.

VII. IMPLEMENTATION AND RESULTS

35. The method was first tested for the reference month December 2003 and then implemented for the reference month January 2004.

An embedded experiment in December 2003

36. We tested the new proposed method for unit price checking as an embedded experiment in the ordinary production process for December 2003. The data were checked using both the old and the new method. The old method, which was not based on a score function, normally flagged about 2,400 observations each month. In the test the old method was modified so that only 1788 observations were flagged. The new method was set to flag 1,000 observations. It was found that 384 of these observations were flagged by both methods. The hit-rate for the observations flagged by the old method was found to be 39% and the hit rate of the new method was 65%. The sum of the corrections in the variable \(Invoiced\ value\) was 494 million SEK for the old method and 819 million SEK for the new method. Corrections of 29 million SEK was found by the old method but not by the new method. On the other hand the new method found corrections of 354 million SEK that the old method didn’t find.
Experiences from the production in 2004

37. Since the result of the test was satisfactory the new method was implemented in production for the reference month of January 2004. Due to needs for cost-cutting the number of edited lines had to be decreased from 2,400 observations to 1,500 observations per month.

When the new method was introduced the hit rate increased from about 40% to about 65% (according to indicator 6). This can be seen in figure 3. The figure shows the total hit rate and the hit rate for the two quantity variables as well as for the variable Invoiced value. As can be seen most of the errors are found on the quantity variable Net Weight.

Despite the decrease in the number of edited observations the impact seems to have increased somewhat. This is illustrated in Figure 4. The impact is here measured by the impact indicator 2. The figure displays the total impact and the impact by variable. Here it is very clear that the two Quantity-variables have the largest errors.

38. The impact for Invoiced value is so low compared to the impact from the other variables that it can hardly be distinguished in figure 4. In figure 5 the impact on the variable invoiced value is displayed without the other variables (indicator 1). It is evident that the impact on Invoiced value has increased with the introduction of the new method.

39. We have changed two of the ten parameters from time to time (N_Obs and P_{imp}) to see if this has an effect on the hit rate and/or on the impact of the errors found. The magnitude of errors in the data varies much between months, making it difficult to say what parameter values are the best.
For the first ten months the Suspicion_Va (Suspicion of Invoiced value relative to suspicion of Quantity) was not used. For the reference month November 2004 an embedded experiment was conducted to see if it was possible to increase the potential impact and hit rate for the variable Invoiced value by including the Suspicion_Va in the Score. The data were checked using both the ordinary method and an extended method where the Suspicion_Va was incorporated.

40. From each method 880 observations were flagged. It was found that 602 observations where flagged by both methods. The results concerning the hit rate are displayed in table 4 below. As can be seen the overall hit rate is somewhat lower for the extended method and the hit rate for one of the quantity-variables is considerably lower. The interesting point however is that the hit rate for the variable Invoiced value doubled from 8% to 16%.

**Table 4.** Hit rates for the experiment for reference month November 2004.
The extended method uses Suspicion_Va (suspicion for Invoiced value relative to suspicion for Quantity) while the ordinary method does not.

<table>
<thead>
<tr>
<th></th>
<th>Ordinary method</th>
<th>Extended method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall</td>
<td>76%</td>
<td>73%</td>
</tr>
<tr>
<td>Quantity 1 (Net weight)</td>
<td>61%</td>
<td>54%</td>
</tr>
<tr>
<td>Quantity 2 (Sup. unit)</td>
<td>13%</td>
<td>12%</td>
</tr>
<tr>
<td>Invoiced value</td>
<td>8%</td>
<td>16%</td>
</tr>
</tbody>
</table>

41. The total impact for the extended method is larger than for the ordinary method but the impact on Invoiced value is in fact smaller for the extended method. This is surprising. The extended method has found many small errors in Invoiced value, but it missed one large erroneous observation. We think it is an accidental occurrence.

**Table 5.** Total value of corrections in Invoiced value and the impact measure for the three variables

<table>
<thead>
<tr>
<th></th>
<th>Ordinary method</th>
<th>Extended method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Difference in thousand SEK</td>
<td>2 558 402</td>
<td>2 488 222</td>
</tr>
<tr>
<td>Impact for Invoiced value</td>
<td>1 692</td>
<td>1 582</td>
</tr>
<tr>
<td>Impact for Quantity 1 (Net weight)</td>
<td>1 356 810</td>
<td>1 355 935</td>
</tr>
<tr>
<td>Impact for Quantity 2 (Sup. unit)</td>
<td>3 791 181</td>
<td>3 795 959</td>
</tr>
<tr>
<td>Total impact</td>
<td>5 149 683</td>
<td>5 153 476</td>
</tr>
</tbody>
</table>

Difference in thousand SEK | 70 180 | 110 | 875 | -4 778 | -3 793

42. In figure 6a can be seen the logarithm of the raw unedited Invoiced values plotted against the logarithm of the edited Invoiced value. The line from the origin with a 45% slope is made up of observations with unchanged Invoiced values. The two lines parallel to this line consists of observations where the unedited values were 10 times too large or 10 times too small.
43. The corresponding picture for net weight is shown in figure 6b. Weights that are ten or thousand times too low or too high seems to be most common but weights that are 100 times too low or too high also exist.

**Figure 6a.** Raw *Invoiced value* plotted against the edited *Invoiced value*

**Figure 6b.** Raw net weight plotted against the edited net weight.

**References**